

Networks Worksheet

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Networks

Guys, networks are awesome.

*Like all labs, I'm just helping you walk through the code — you gotta figure out the rest of the worksheet on your own.

Download the code*

<https://git.io/vDSzh>

Also download the data

<https://git.io/vDSgT>

**Let's first walk through the function we
gave you again.**

**You really don't need to know this. This is entirely for
your own personal edification.**

Code review — networkPractical()

```
networkPractical <- function(network, attackRate, acquireImmunity, runTime) {  
  
  #we will encode susceptible individuals as 0, infected as 1, immune as 2  
  numberOfPeople <- network.size(network) #size of the population  
  #start out with everyone susceptible  
  statusList <- array(0,dim=c(numberOfPeople,1))  
  timeSeries <- NULL  
  keepStatus <- NULL  
  
  #INFECT THE FIRST PERSON!  
  statusList[1] <- 1  
}
```

networkPractical just takes a few arguments.

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networkPractical just takes a few arguments.

- network is a network object that you give it
- attackRate is the probability of infection between an I and an S (conditional on them being connected by an edge)
- acquireImmunity is the probability of gaining immunity after infection

Code review — networkPractical()

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  #INFECT THE FIRST PERSON!  
  statusList[1] <- 1  
}
```

`networkPractical` just takes a few arguments.

- `network` is a network object that you give it
- `attackRate` is the probability of infection between an I and an S (conditional on them being connected by an edge)
- `acquireImmunity` is the probability of gaining immunity after infection
- `runTime` is just how long you want to run the simulation.

Code review — networkPractical()

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  numberOfPeople <- network.size(network) #size of the population  
  #start out with everyone susceptible  
  statusList <- array(0,dim=c(numberOfPeople,1))  
  timeSeries <- NULL  
  keepStatus <- NULL  
  
  #INFECT THE FIRST PERSON!  
  statusList[1] <- 1
```

First, just find the number of people in your population (in this case, the network)

Code review — networkPractical()

```
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  #we will encode susceptible individuals as 0, infected as 1, immune as 2  
  numberOfPeople <- network.size(network) #size of the population }}  
  #start out with everyone susceptible  
  statusList <- array(0,dim=c(numberOfPeople,1))  
  timeSeries <- NULL  
  keepStatus <- NULL  
  
  #INFECT THE FIRST PERSON!  
  statusList[1] <- 1
```

Then we are going to make a list that contains the status of each node. We will it up with 0 because everybody is susceptible. (Here, we are just declaring the number of dimensions to be 1 column with as many rows as there are people).

Code review — networkPractical()

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  #start out with everyone susceptible  
  statusList <- array(0,dim=c(numberOfPeople,1)) }}  
  timeSeries <- NULL  
  keepStatus <- NULL  
  
  #INFECT THE FIRST PERSON!  
  statusList[1] <- 1
```

We just make two other objects (empty) that we will use later in our loops. (Recall from previous labs that if you make an object inside of a loop, it gets overwritten every time you run it.)

Code review — networkPractical()

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  numberOfPeople <- network.size(network) #size of the population }}  
  #start out with everyone susceptible  
  statusList <- array(0,dim=c(numberOfPeople,1))  
  timeSeries <- NULL  
  keepStatus <- NULL  
  
  #INFECT THE FIRST PERSON!  
  statusList[1] <- 1
```

Infect somebody. In this case, we are infecting the first person, but we could also just infect somebody randomly. We use 1 to signify infected (recall 0 is for susceptibles).

Code review — networkPractical()

```
for(time in 1:runTime) {  
  print(time)  
  
  whoIsInfected <- which(statusList==1)  
  whoIsImmune <- which(statusList==2)  
  
  if(length(whoIsInfected)==numberOfPeople |  
      length(whoIsImmune)==numberOfPeople |  
      length(whoIsInfected)==0) {}  
}
```

Now we get to the good stuff. We are going to run a `for()` loop for as many timesteps as specified in `runTime`. We print it just so we have some idea of whether or not the loop is going.

Code review — networkPractical()

```
for(time in 1:runTime) {  
  print(time)  
  
  whoIsInfected <- which(statusList==1)  
  whoIsImmune <- which(statusList==2)  
  
  if(length(whoIsInfected)==numberOfPeople |  
     length(whoIsImmune)==numberOfPeople |  
     length(whoIsInfected)==0) {}  
}
```

Recall from previous labs that `which()` just returns the **index** (row-number in this case) for which the condition is true. So we are asking `whoIsInfected`? And we get back a list that tells us which row has an infected status 1. (Also recall that each row represents a node or person so in this case you can think of it as an ID as well.)

Code review — networkPractical()

```
for(time in 1:runTime) {  
  print(time)  
  
  whoIsInfected <- which(statusList==1)  
  whoIsImmune <- which(statusList==2)  
  
  if(length(whoIsInfected)==numberOfPeople |  
      length(whoIsImmune)==numberOfPeople |  
      length(whoIsInfected)==0) {}  
}
```

Recall from previous labs that `which()` just returns the **index** (row-number in this case) for which the condition is true. So we are asking `whoIsInfected`? And we get back a list that tells us which row has an infected status 1. (Also recall that each row represents a node or person so in this case you can think of it as an ID as well.)

Obviously, the first time you run this, nobody will be Immunte and only one (the one we assign) will be infected, but it changes each time we go through the `for` loop.

Code review — networkPractical()

```
for(time in 1:runTime) {  
  print(time)  
  
  whoIsInfected <- which(statusList==1)  
  whoIsImmune <- which(statusList==2)  
  
  if(length(whoIsInfected)==numberOfPeople |  
     length(whoIsImmune)==numberOfPeople |  
     length(whoIsInfected)==0) {}  
}
```

This is just creating a stop condition. The pipe | means *or*. If (1) everybody is infected or (2) everybody is immune or (3) nobody is infected, then run what is inside the bracket. Since nothing is in the bracket, it will break out of the loop.

Code review — networkPractical()

```
else {  
  for(i in 1:length(whoIsInfected)){ #only look at people who are infected  
    #see who is connected to infected node  
    contacts <- get.neighborhood(network, whoIsInfected[i])  
    #see which contacts are susceptible to infection  
    suscContacts <- which(statusList[contacts]==0)
```

That's all boring though. This section starts what to do if you have both infected and susceptibles.

Go through everybody who is infected. Get all their contacts (`get.neighborhood`) and then find the ones that are susceptible.

Code review — networkPractical()

```
if(length(suscContacts)>0) {  
  #see which infectious contacts lead to infection  
  successfulInfect <- which(runif(length(suscContacts))<attackRate)  
  
  if(length(successfulInfect)>0){  
    #INFECT SUSCEPTIBLES!  
    statusList[contacts[suscContacts[successfulInfect]]] <- 1  
  }  
}
```

If there are any that are susceptible (that is, if `length(suscContacts) > 0`), try to infect them. Here, we use a random uniform (`runif`) to draw a number between $[0, 1]$. If that number is less than our attack rate, we infect them. Otherwise, we do nothing.

The second half then says, if anybody was infected (`successfulInfect`), change their status to 1 to indicate they were infected.

Code review — networkPractical()

```
if(length(whoIsInfected)>0){  
  #see who becomes immune  
  becomeImmune <- which(runif(length(whoIsInfected)) < acquireImmunity)  
  statusList[whoIsInfected[becomeImmune]] <- 2  
}
```

Now let's look at everybody who is infected, and again, randomly assign them to immune using the `runif`. This is the same as above, just using the random uniform number to assign immunity instead of infection.

Code review — networkPractical()

```
S <- length(which(statusList==0))
I <- length(which(statusList==1))
R <- length(which(statusList==2))
timeSeries <- rbind(timeSeries,c(S,I,R)) #keep track of people
keepStatus <- cbind(keepStatus,statusList)
```

Now, every time we do this loop (remember we are doing this `runTimes` many times), record the number of susceptible, infected, and recovered. Then bind that to the `timeSeries` object we made above. Similarly, keep track of all the statuses for every timestep in the `keepStatus` object.

Question 1: Install the network package

You got this one.

But in case you don't:

```
## Install it  
install.packages("network")  
  
## Load it  
library(network)
```

Question 2: Import the networks

You got this one too

Remember, the GUI is your friend.

```
library(readr)

blah <- read_delim("./data/network1.txt", delim = " ",
                  col_names = FALSE, trim_ws = TRUE)
mat1 <- read_delim("./data/mat1-1.txt", delim = " ",
                  col_names = FALSE, trim_ws = TRUE)
mat3 <- read_delim("./data/mat1-3.txt", delim = "\t",
                  col_names = FALSE, trim_ws = TRUE)
mat4 <- read_delim("./data/mat3.txt", delim = "\t",
                  col_names = FALSE, trim_ws = TRUE)
matBA <- read_delim("./data/ba_net.txt", delim = " ",
                   col_names = FALSE, trim_ws = TRUE)
```

NOTE: Some of these are delimited with a tab ("\t") and some are whitespace delimited (" "). Use the GUI so you can see a live preview and modify accordingly. Also don't forget there are no headers.

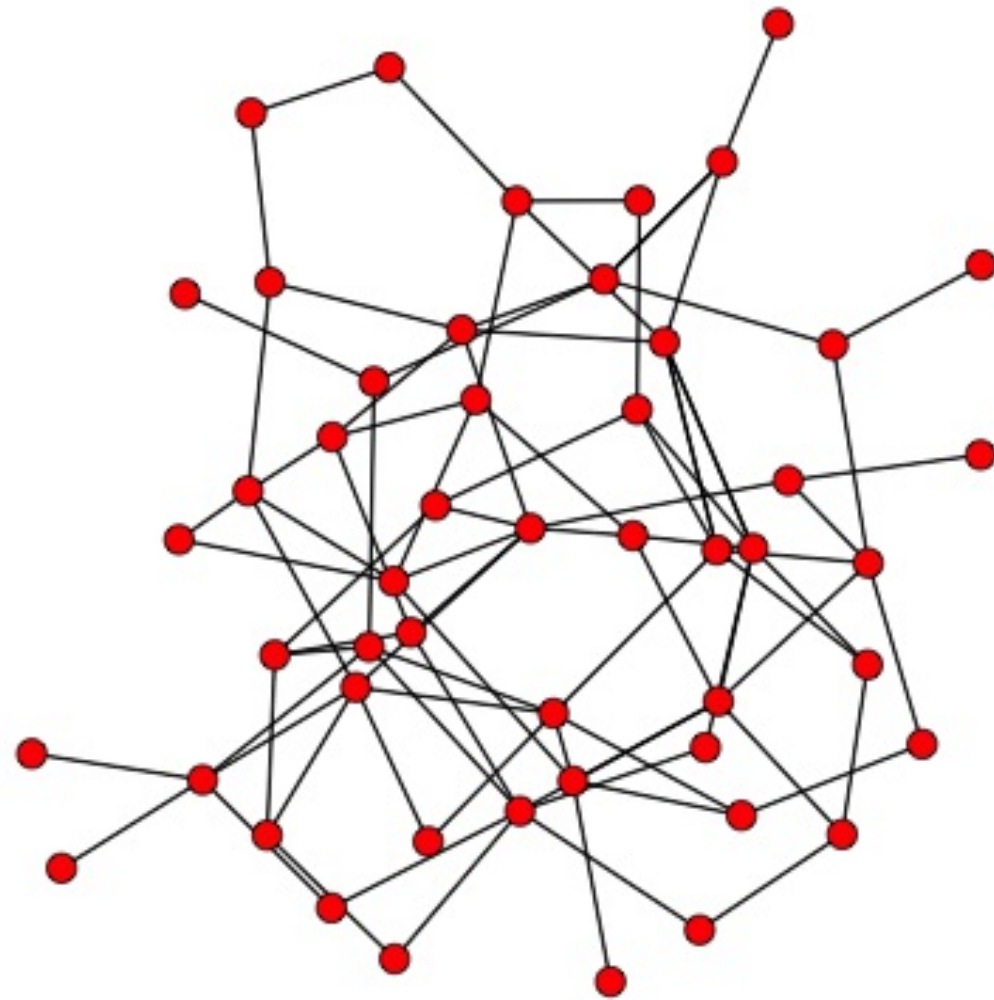
Convert them to networks

```
net1 <- as.network(blah, directed = FALSE)
net3 <- as.network(mat3, directed = FALSE)
net4 <- as.network(mat4, directed = FALSE)

## Note: These have nodes labeled 0. We need to add 1
## so that the zeros are not there.
mat1 <- mat1 + 1
matBA <- matBA + 1
net2 <- as.network(mat1, directed = FALSE)
netBA <- as.network(matBA, directed = FALSE)
```

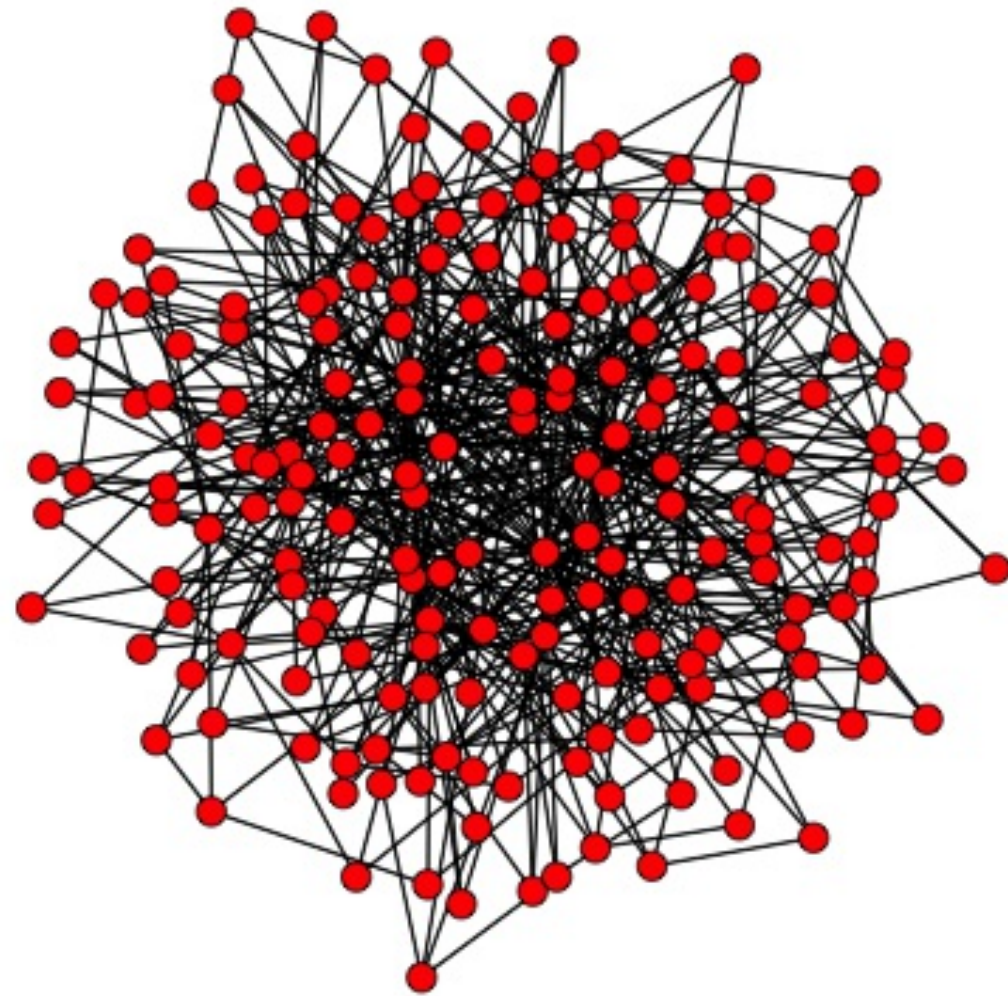
Plot the networks — net1

```
plot.network(net1, vertex.cex = 1.5)
```



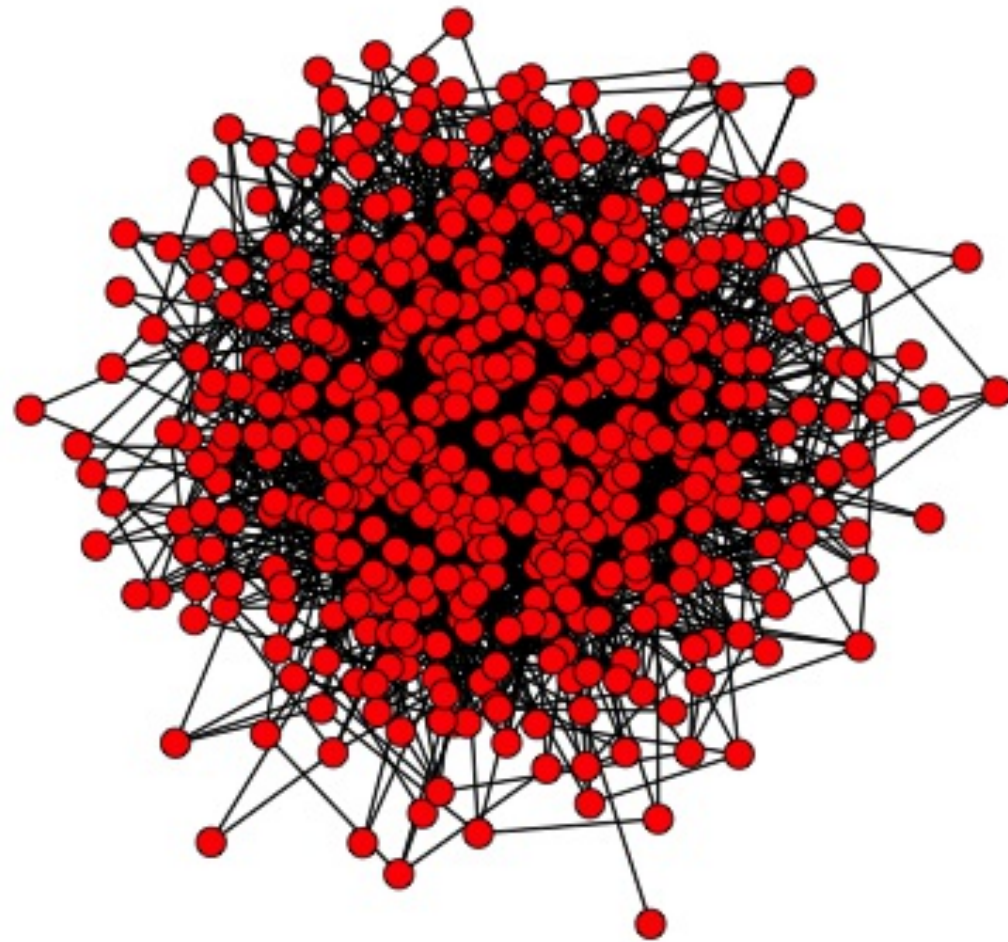
Plot the networks — net2

```
plot.network(net2, vertex.cex = 1.5)
```



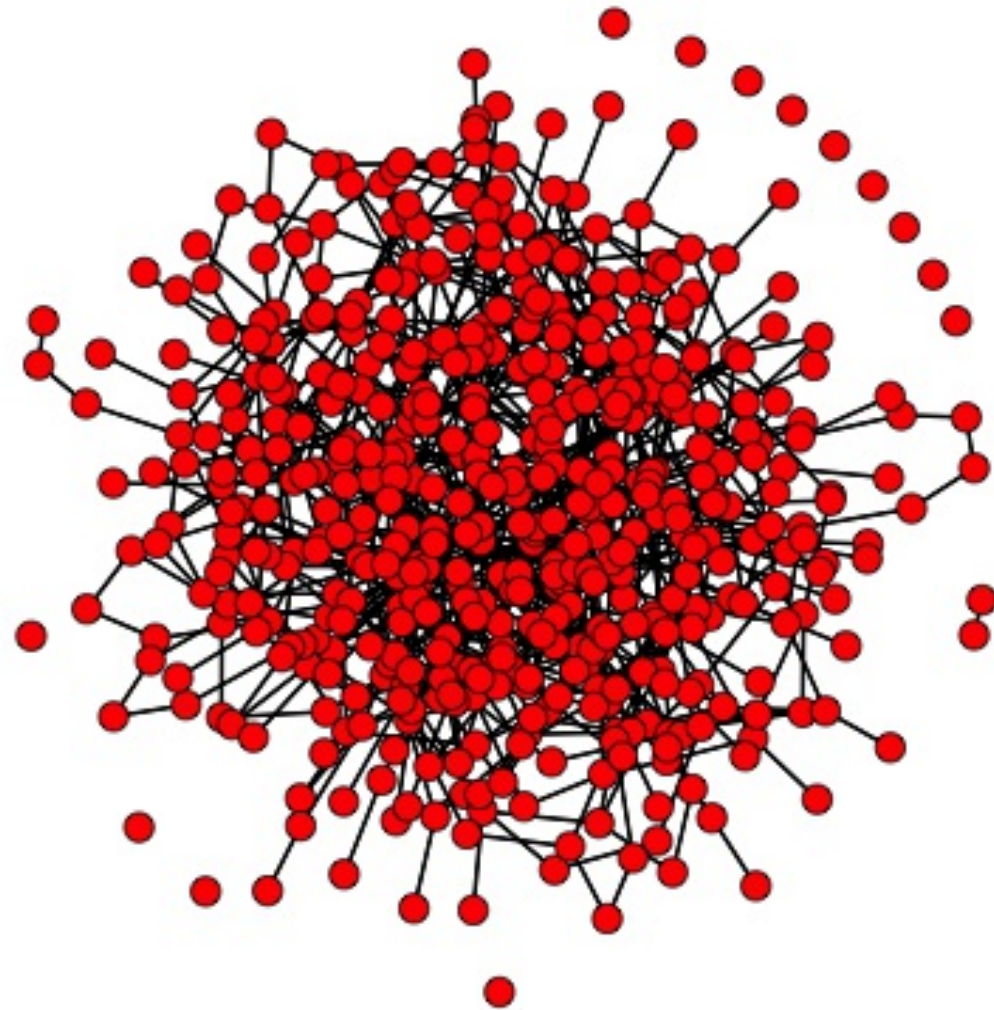
Plot the networks — net3

```
plot.network(net3, vertex.cex = 1.5)
```



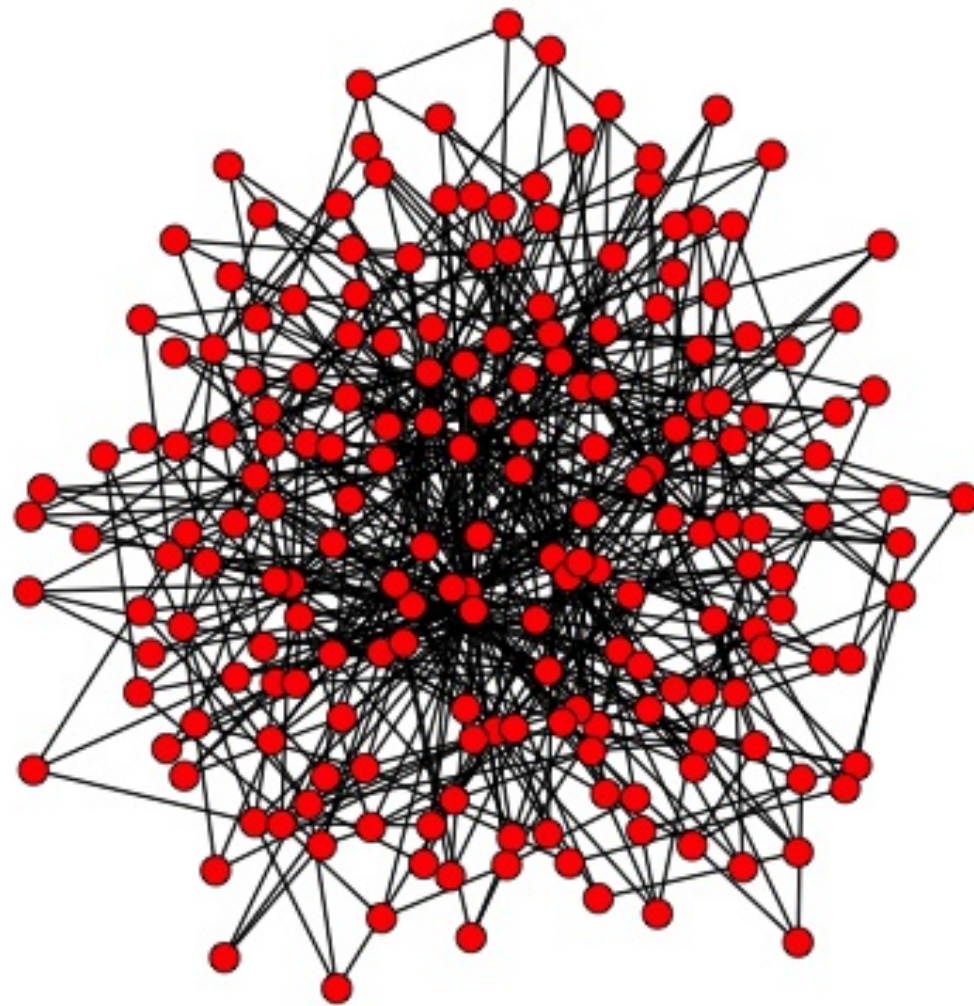
Plot the networks — net4

```
plot.network(net4, vertex.cex = 1.5)
```



Plot the networks — netBA

```
plot.network(netBA, vertex.cex = 1.5)
```



What's the point?

What's the point?

Hopefully, it's clear by looking at the plots of the networks what we want to learn here. How does the structure of the network affect disease dynamics? What about networks with isolates and more than one connected component? What about dense vs sparse networks?

Question 3. Degree distributions

What's this code do?

```
deg <- NULL
for(i in 1:network.size(net1)) {
  deg <- rbind(deg, length(get.neighborhood(net1, i)))
}
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What's this code do?

```
deg <- NULL
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}
```

- For every node in the network...
- Go through and get the number of neighbors (`length(get.neighborhood())`).

What's this code do?

```
deg <- NULL
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}
```

- For every node in the network...
- Go through and get the number of neighbors (`length(get.neighborhood())`).
- And append it to an object called `deg`.

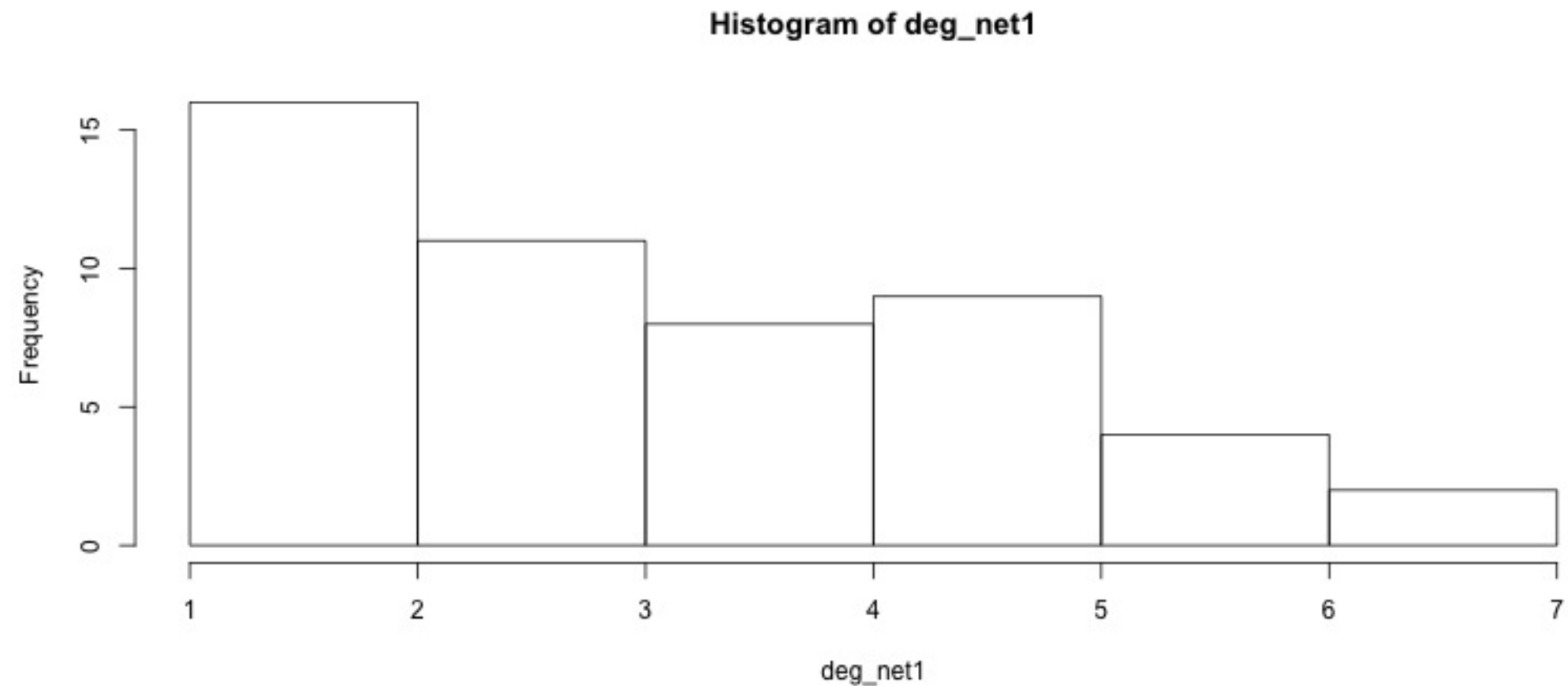
What's this code do?

```
deg <- NULL
for(i in 1:network.size(net1)) {
  deg <- rbind(deg, length(get.neighborhood(net1, i)))
}
```

- For every node in the network...
- Go through and get the number of neighbors (`length(get.neighborhood())`).
- And append it to an object called `deg`.
- That's it. Just get the number of neighbors for every node in a network.

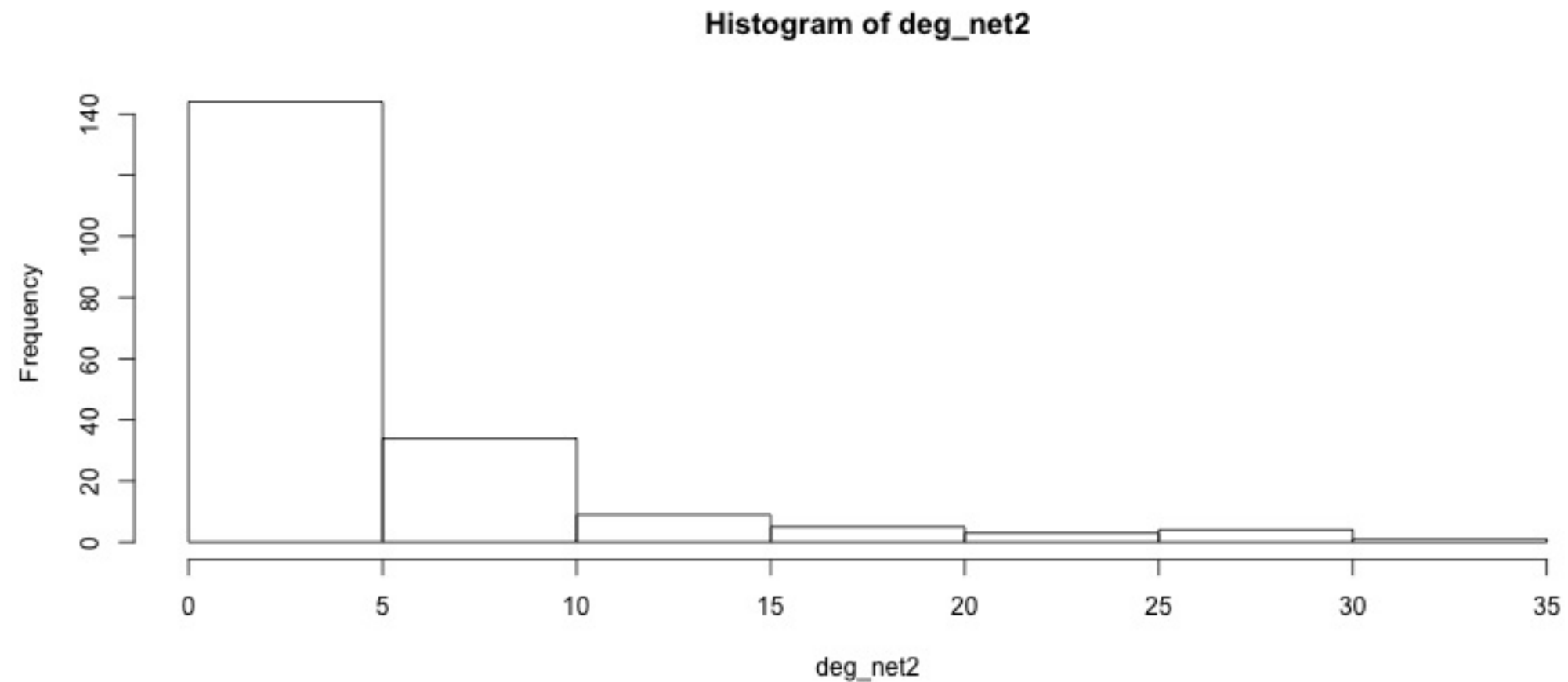
Degree distribution — net1

```
deg_net1 <- NULL
for(i in 1:network.size(net1)) {
  deg_net1 <- rbind(deg_net1, length(get.neighborhood(net1, i)))
}
hist(deg_net1)
```



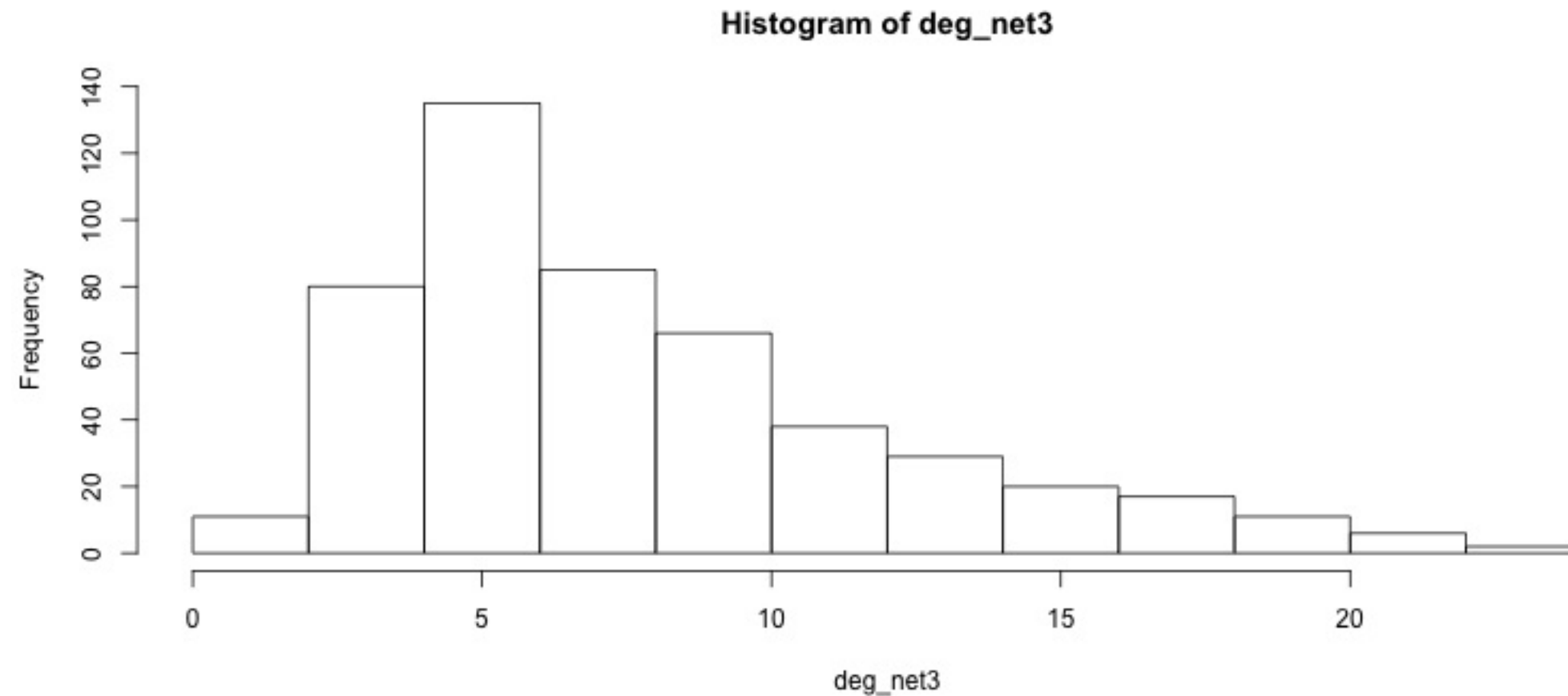
Degree distribution — net2

```
deg_net2 <- NULL
for(i in 1:network.size(net2)) {
  deg_net2 <- rbind(deg_net2, length(get.neighborhood(net2, i)))
}
hist(deg_net2)
```



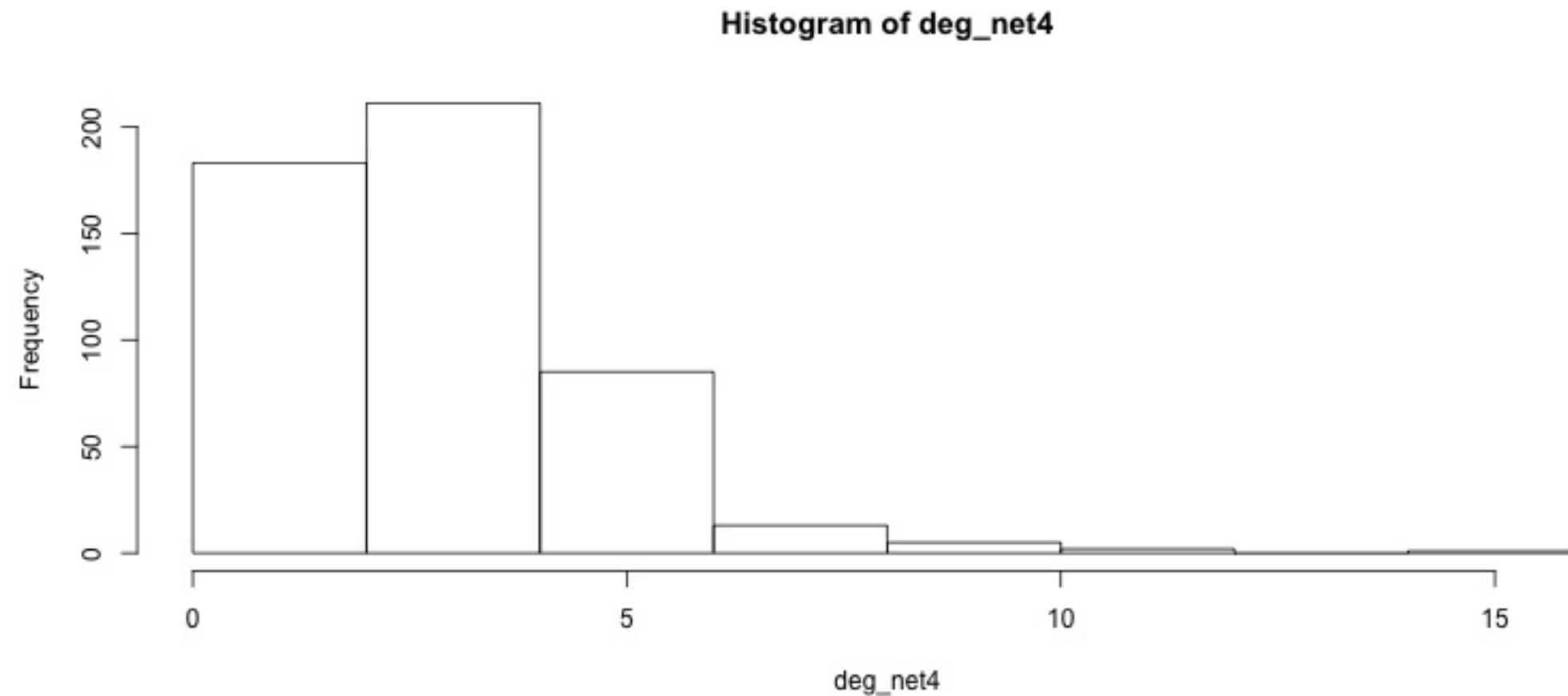
Degree distribution — net3

```
deg_net3 <- NULL
for(i in 1:network.size(net3)) {
  deg_net3 <- rbind(deg_net3, length(get.neighborhood(net3, i)))
}
hist(deg_net3)
```



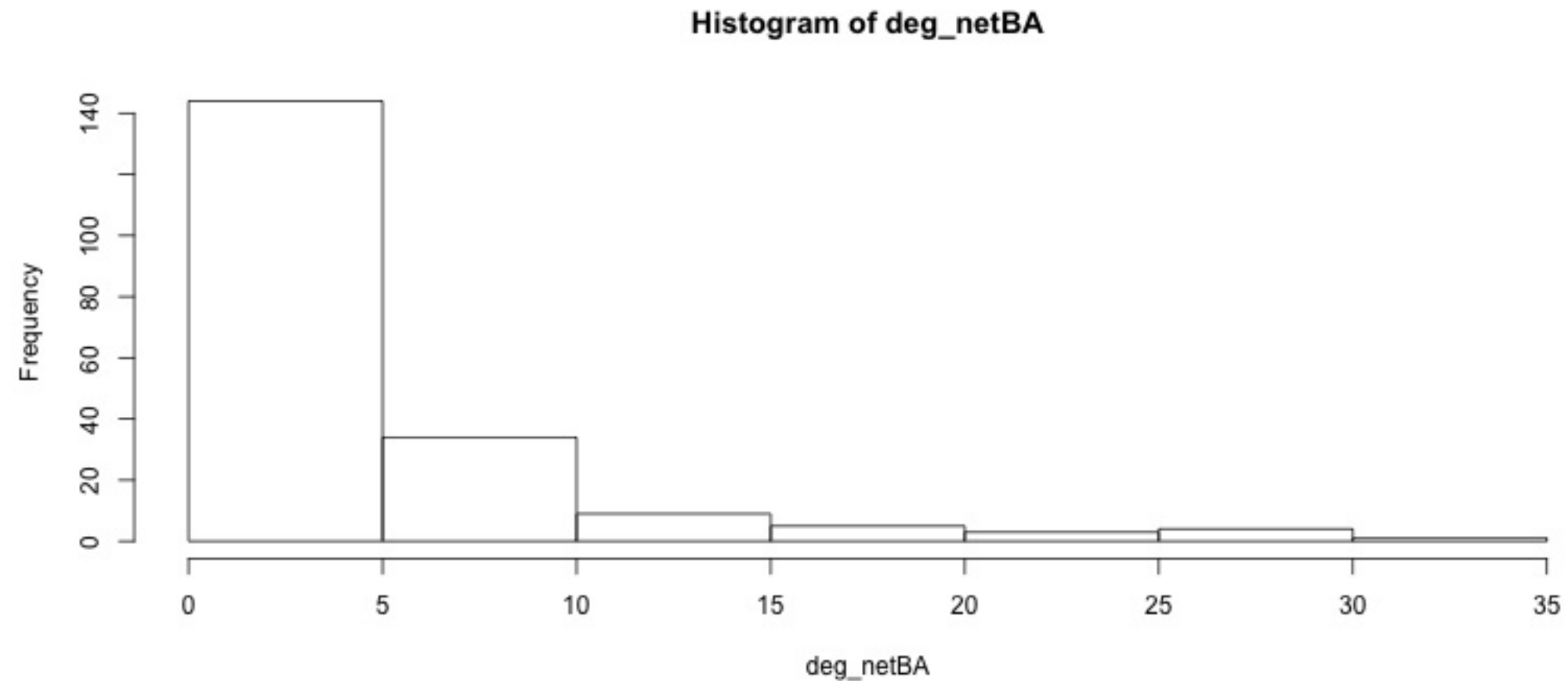
Degree distribution — net4

```
deg_net4 <- NULL
for(i in 1:network.size(net4)) {
  deg_net4 <- rbind(deg_net4, length(get.neighborhood(net4, i)))
}
hist(deg_net4)
```



Degree distribution — netBA

```
deg_netBA <- NULL
for(i in 1:network.size(netBA)) {
  deg_netBA <- rbind(deg_netBA, length(get.neighborhood(netBA, i)))
}
hist(deg_netBA)
```

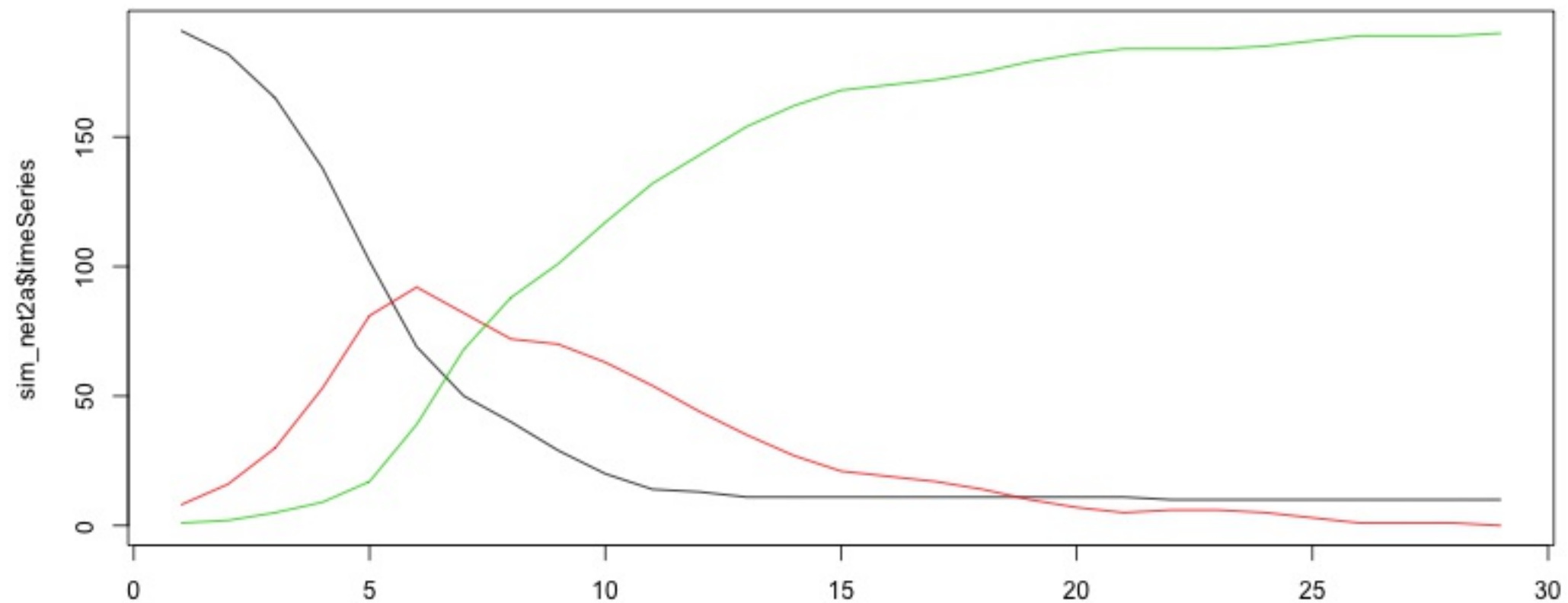


Question 4. Simulating on a network

Simulate on net2

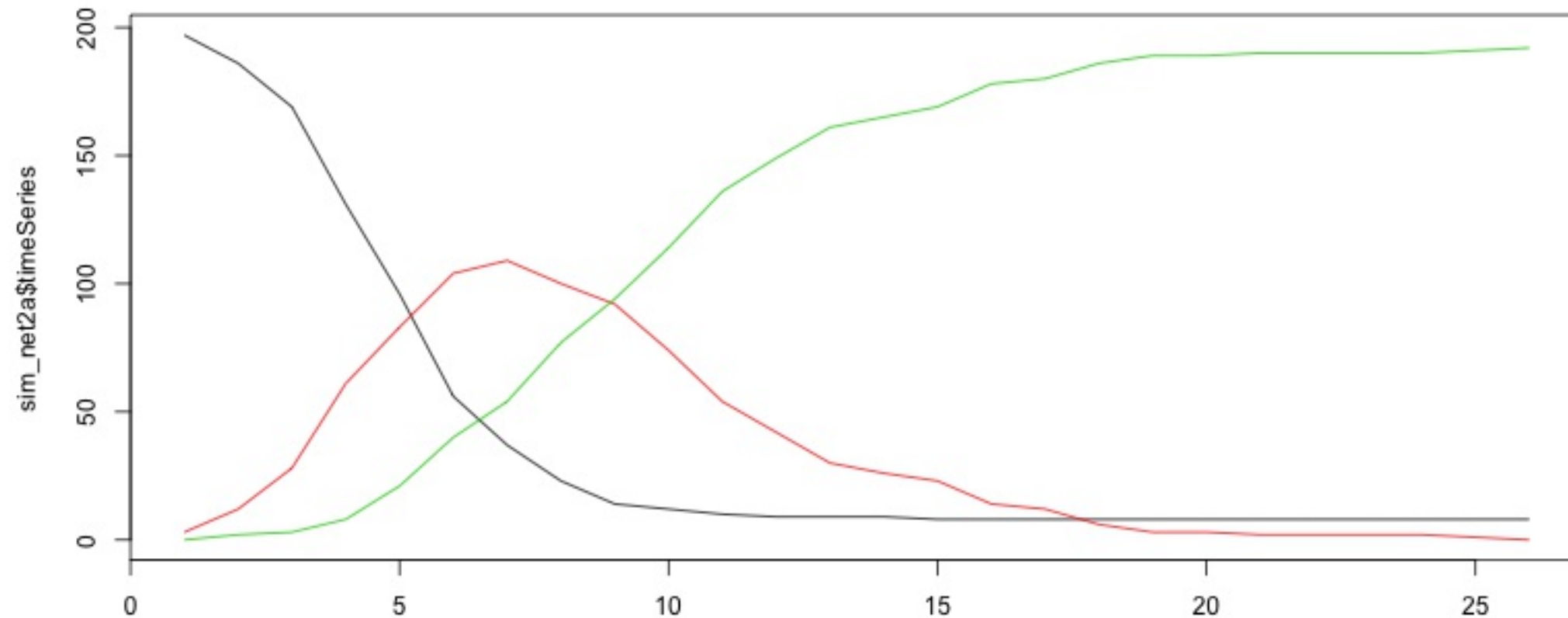
```
sim_net2a <- networkPractical(network = net2, attackRate = .2,  
                             acquireImmunity = .2, runTime = 50)
```

```
matplot(sim_net2a$timeSeries, type = "l", lty = 1)
```



Simulate on net2

```
matplot(sim_net2a$timeSeries, type = "l", lty = 1)
```

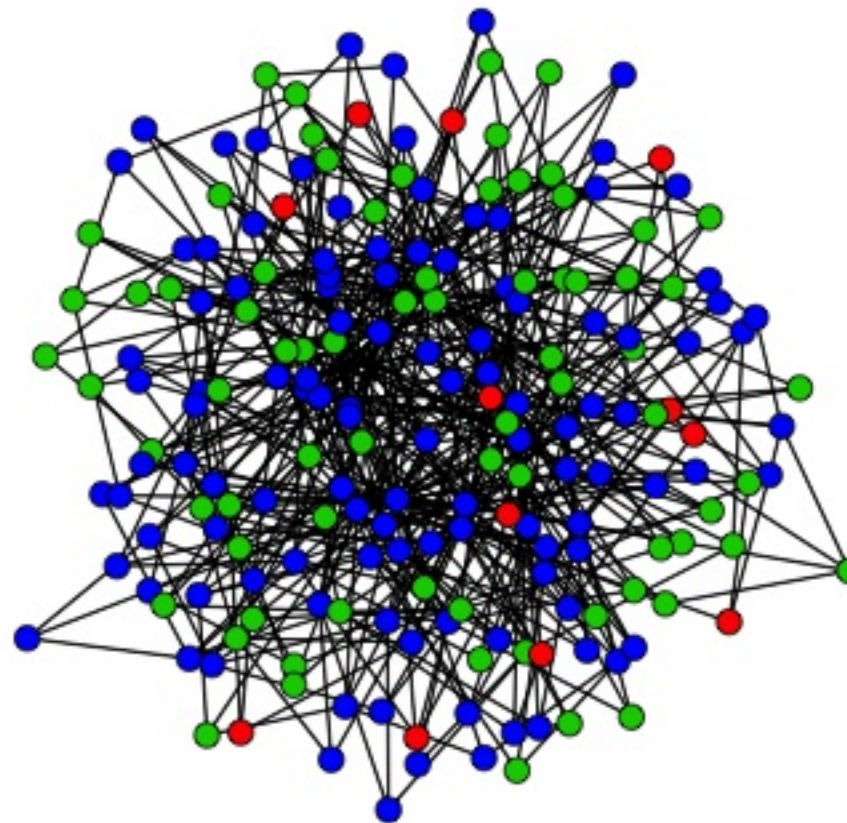


NOTE: Every run results in a different plot. Why?

Question 5. Plot the network with node status

Plot with status

```
plot.network(net2, vertex.col = sim_net2a$status[, 10] + 2,  
            vertex.cex = 1.5)  
legend("topright", fill = c(2, 3, 4), legend = c("S", "I", "R"))
```



Questions 6 - 9

Just use previous slides with different parameters. Change timesteps. Plot two infectious curves on the same plot. Play with it a bit. We give you the code so you can play with the numbers and see what happens. Don't worry about the code too much.

That's it.

Thanks